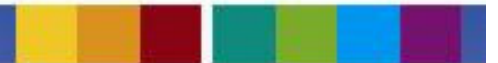




Discrimination metrics for sensory panel data

Chris Crocker



- Most common measure in sensometrics

For panel means

$$F = \frac{MS(\text{Product})}{MS(\text{Assessor} \times \text{Product})}$$

Expected mean squares (balanced design)

$$E(MS_{\text{Product}}) = Q + n_R \text{Var}(\text{Assessor} \times \text{Product}) + \text{Var}(\text{rep})$$

$$E(MS_{\text{Assessor} \times \text{Product}}) = n_R \text{Var}(\text{Assessor} \times \text{Product}) + \text{Var}(\text{rep})$$

- Interpretation not very intuitive
- Metric on non-linear scale



- Used in biometrics, psychometrics, etc.
- Assume independence of product and error variances:

$$\text{Var}(\textit{measurement}) = \text{Var}(\textit{product}) + \text{Var}(\textit{error})$$

- Intraclass Correlation Coefficient

$$r = \frac{\text{Var}(\textit{product})}{\text{Var}(\textit{measurement})}$$

- Proportion of observed variance attributable to sample variation
 - proportion of “signal” in data
- More interpretable than F-ratio but highly non-linear
- Extendible to PCA and PLS

- Transform ICC to a linear metric

Wheeler, D.J. and Lyday, R.W. (1989). Evaluating the Measurement Process, 2nd edition, SPC Press Inc.

$$D_R = \sqrt{\frac{1+r}{1-r}}$$

- number of distinct categories of product that can be established

DR ~ 2 threshold of usefulness

DR ~ 3 moderate discrimination

DR > 4 high discrimination

- Suggestion: ignore attributes with DR < 1.75 (ICC ~ 0.50)

Sample F-ratio typically just significant for dataset of 8-12 products and 10 assessors

Example – salad dressing data

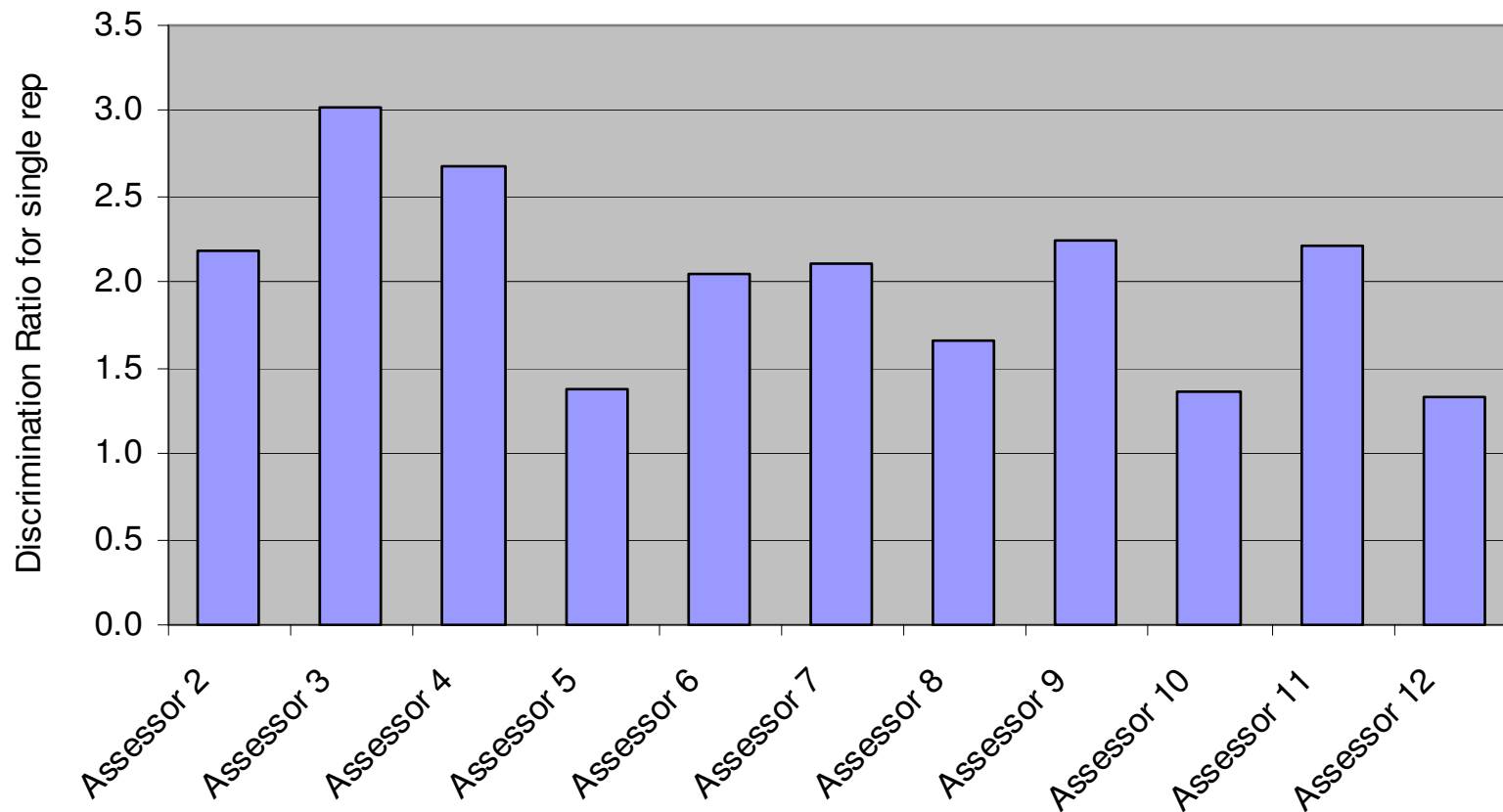


- Discrimination of assessors
 - $\text{Var}(\text{error})$ estimated from replicates
 - Prefer value based on a single rep
- Discrimination of panel means
 - $\text{Var}(\text{error})$ estimated from Assessor x Sample interaction
- Discrimination of PCA dimensions
 - Propagate errors into principal components
 - Requires error covariances
 - Can also do for PLS factors



All panellists have $p < 0.01$

Discrimination of panellists on Sour Flavour

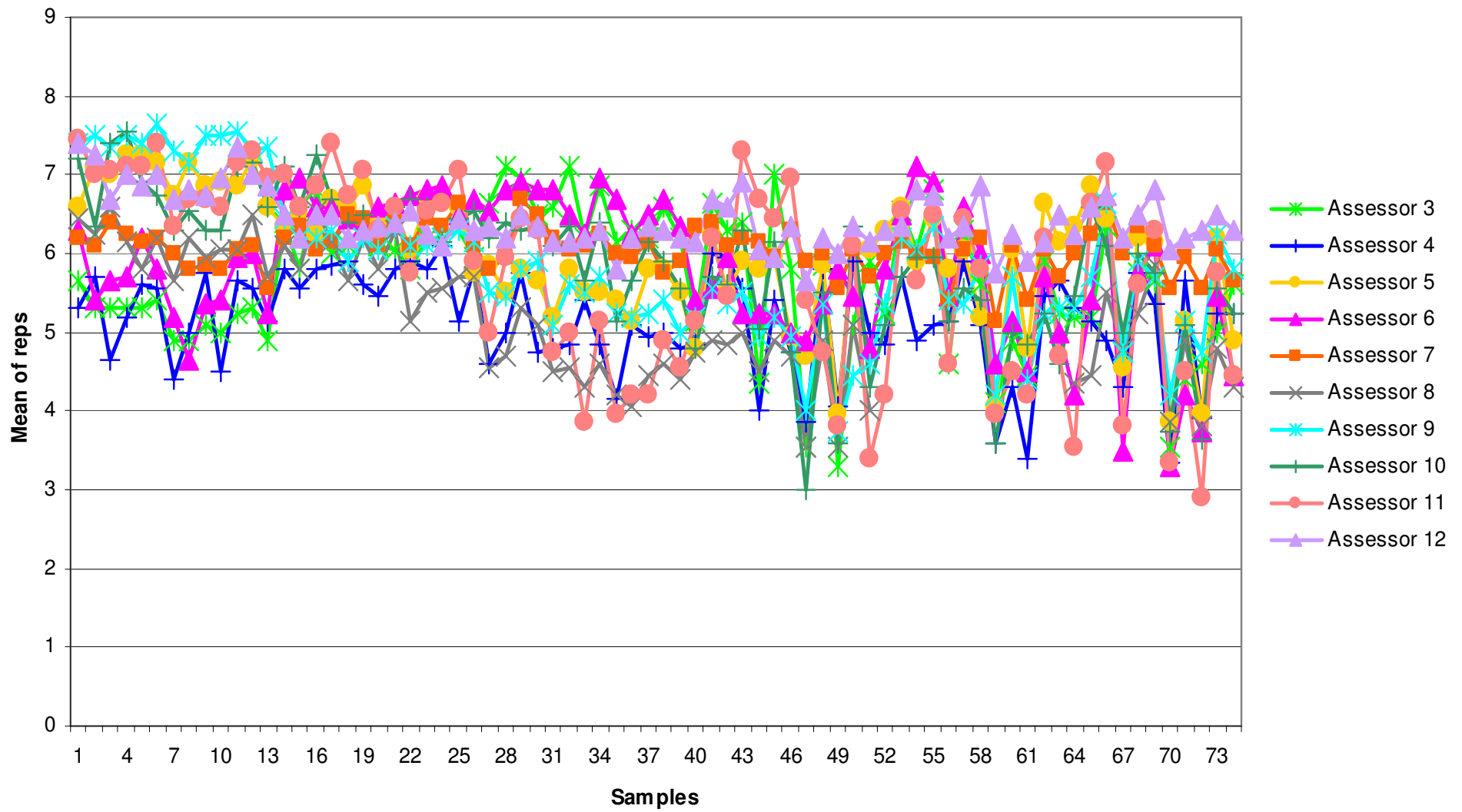


Discrimination of panel means

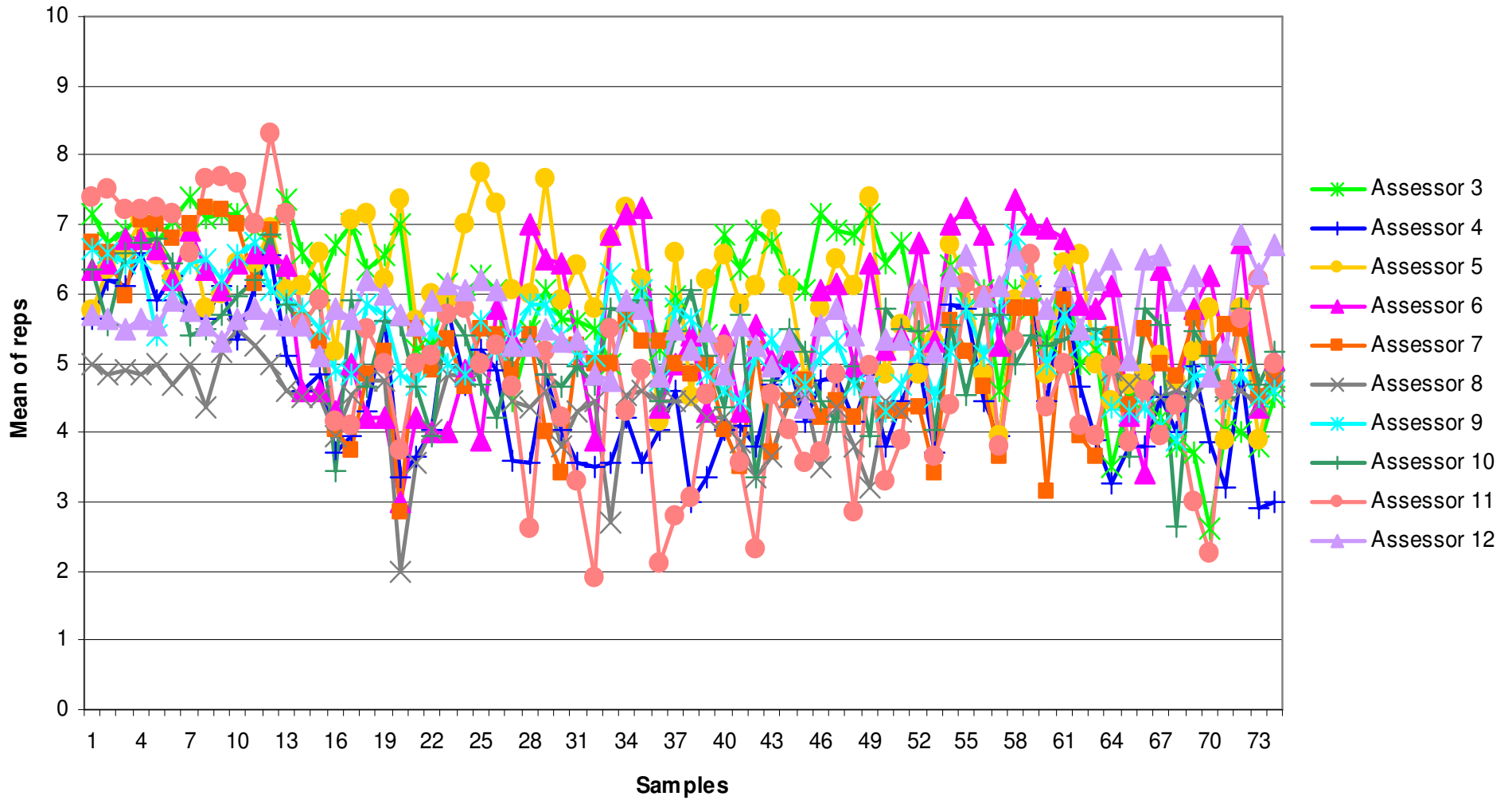


Attribute	Intraclass Correlation Coefficient	Discrimination Ratio
Acidic Odour	0.95	6.4
Sour Odour	0.93	5.1
Fresh Odour	0.97	8.1
Rancid Odour	0.97	8.1
Off-Odour	0.93	5.3
Whiteness	0.90	4.4
Colour, Hue	0.87	3.8
Colour Intensity	0.93	5.1
Mustard Flavour	0.87	3.8
Acidic Flavour	0.96	7.0
Sour Flavour	0.84	3.3
Sweetness	0.62	2.1
Fresh Flavour	0.97	7.9
Rancid Flavour	0.97	8.4
Off-Flavour	0.94	5.7

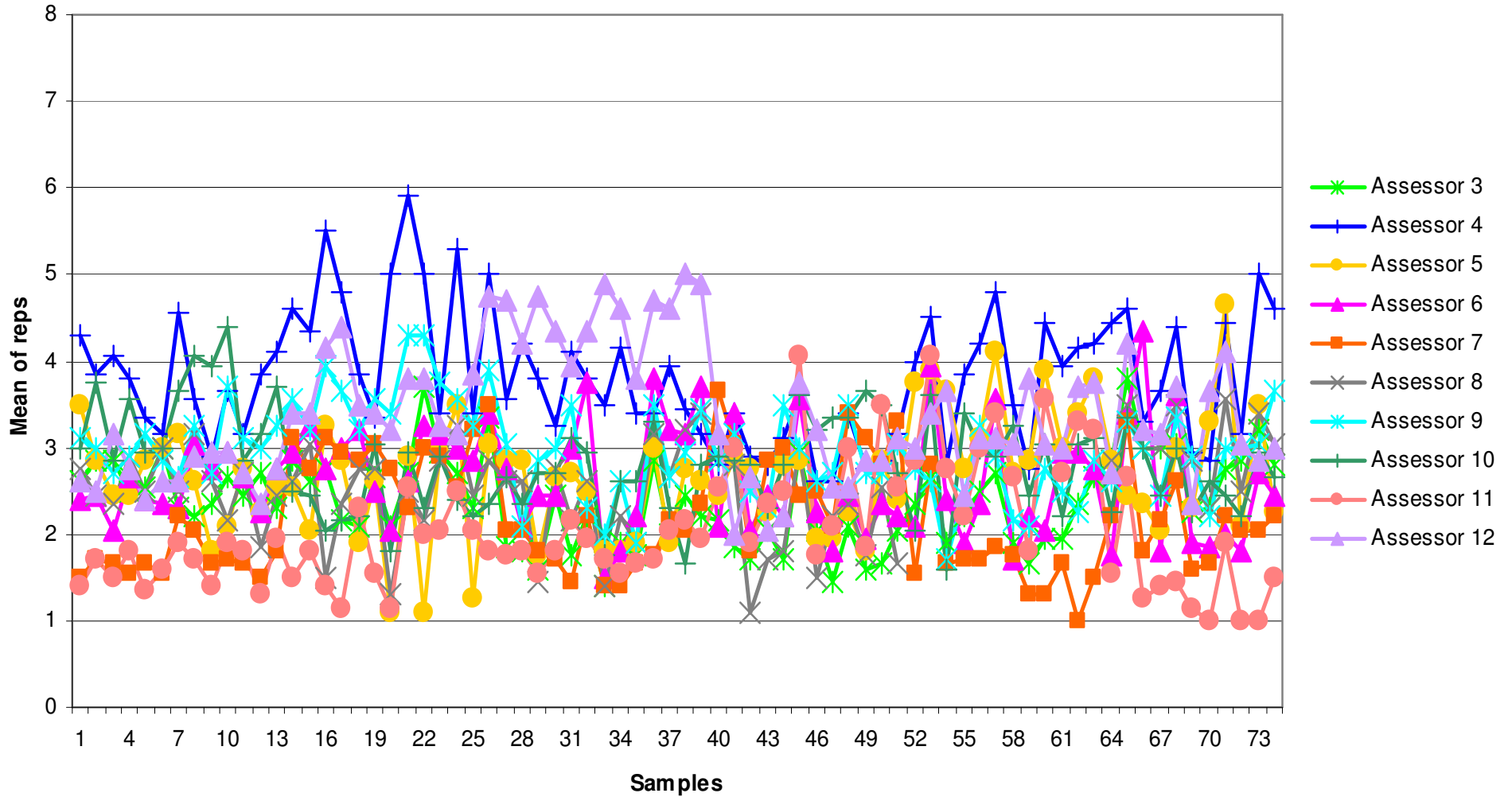
Assessor x Sample interaction plot for Whiteness (DR=4.4)



Assessor x Sample interaction plot for Sour Flavour (DR=3.3)



Assessor x Sample interaction plot for Sweetness (DR=2.05)

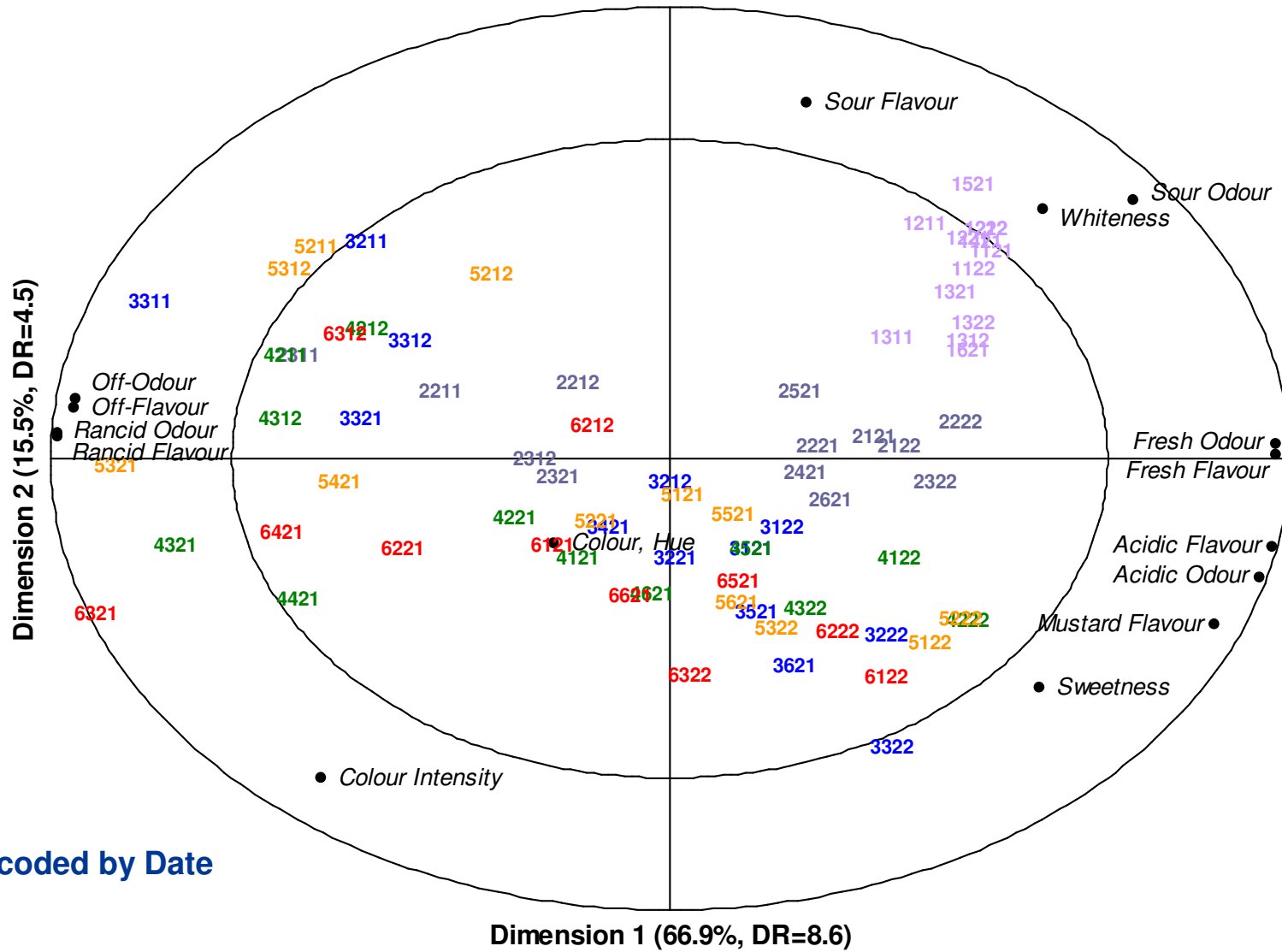


PCA of salad dressing data - correlation matrix



Dimension	Variance	ICC	Discrimination Ratio
1	66.9%	0.97	8.6
2	15.5%	0.91	4.5
3	11.2%	0.89	4.2
4	2.7%	0.49	1.7
5	1.5%	0.34	1.4
6	0.7%	0.04	1.0
7	0.6%	0.31	1.4
8	0.3%	0.00	1.0
9	0.2%	0.00	1.0
10	0.1%	0.00	1.0
11	0.1%	0.00	1.0
12	0.1%	0.00	1.0
13	0.0%	0.00	1.0
14	0.0%	0.00	1.0

PCA map of first 2 dimensions



- Discrimination Ratio provides a linear, intuitive metric
 - communicable to non-statisticians
- Interpretation robust to distributional assumptions
- Applicable to functions of the attributes e.g. principal components
- Knowledge of Intraclass Correlation Coefficient useful in modelling
- Details in poster

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